

TRIGONOMETRIC IDENTITIES

Evaluate the following

1 . $2 \sin^2 30^\circ - 3 \cos^2 45^\circ + \tan^2 60^\circ$.

2 . $\tan 48^\circ \tan 23^\circ \tan 42^\circ \tan 67^\circ$

3 . $\cos 90^\circ \sin 0^\circ - \sin 0^\circ \cos 90^\circ$

4 . $\sin^2 20^\circ + \sin^2 70^\circ - \tan^2 45^\circ$

5. $\frac{\tan^2 60^\circ + 4 \cos^2 45^\circ + 3 \sec^2 30^\circ + 5 \cos^2 90^\circ}{\operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}$

6. $\frac{\sec 70^\circ}{\operatorname{cosec} 30^\circ} + \frac{\sin 59^\circ}{\cos 31^\circ}$

7. $\frac{\cos^2 20^\circ + \cos^2 70^\circ}{\sin^2 59^\circ + \sin^2 31^\circ} + \sin 35^\circ \sec 55^\circ$

8. $\operatorname{cosec}(65^\circ + \theta) - \sec(25^\circ - \theta) - \tan(55^\circ - \theta) + \cot(35^\circ + \theta)$

9. If $4 \tan A = 3$, then find the value of $\frac{\cos A - \sin A}{\cos A + 2 \sin A}$

10. Find value of K , if $\frac{\cos 20^\circ}{\sin 70^\circ} + \frac{2 \cos \theta}{\sin(90^\circ - \theta)} = \frac{k}{2}$

11. Evaluate $\left(\frac{3 \cos 43^\circ}{\sin 47^\circ}\right)^2 - \frac{\cos 37^\circ \operatorname{cosec} 53^\circ}{\tan 5^\circ \tan 25^\circ \tan 45^\circ \tan 65^\circ \tan 85^\circ}$

12. If $\sin(A - B) = 0$, $\cos(A + B) = 0$ find value of A and B, where A and B are acute angle .

13. If $\tan(A + B) = \sqrt{3}$, and $\tan(A - B) = 0$, find value of A and B , where A and B are acute angles.

14. if $\sec 2A = \operatorname{cosec}(A - 42^\circ)$, where 2A is an acute angle, find value of A.

15. simplify : $(1 + \tan^2 A) (1 - \sin A) (1 + \sin A)$

16. If A, B and C are the interior angles of a triangle ABC, then show that $\tan\left(\frac{B+C}{2}\right) = \cot \frac{A}{2}$

17. If $\sin(2A + 45^\circ) = \cos(30^\circ - A)$, find value of A .

PROVE THE IDENTITIES

18. $\tan^4 A + \tan^2 A = \sec^4 A - \sec^2 A$

19. $(\operatorname{cosec} A - \sin A)(\sec A - \cos A)(\tan A + \cot A) = 1$

20. $\tan A + \cot A = \sec A \operatorname{cosec} A$

$$21. \sqrt{\frac{1-\cos\theta}{1+\cos\theta}} = \operatorname{cosec}\theta - \cot\theta$$

$$22. \frac{1}{\operatorname{cosec}A - \cot A} - \frac{1}{\sin A} = \frac{1}{\sin A} - \frac{1}{\operatorname{cosec}A + \cot A}$$

$$23. (\sec A - \tan A)^2 = \frac{1 - \sin A}{1 + \sin A}$$

$$24. (\sin A + \operatorname{cosec}A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$$

$$25. \frac{\cos A}{1 + \sin A} + \frac{1 + \sin A}{\cos A} = 2 \sec A$$

$$26. \frac{\cot A + \operatorname{cosec}A - 1}{\cot A - \operatorname{cosec}A + 1} = \frac{1 + \cos A}{\sin A}$$

$$27. \text{ If } \sin\theta + \cos\theta = \sqrt{3} \text{ then prove that } \tan\theta + \cos\theta = 1$$

$$28. \text{ If } \sin(A - B) = \frac{1}{2} \text{ and } \cos(A + B) = \frac{1}{2} \text{ if } 0 < A + B \leq 90^\circ, A < B \text{ find } A \text{ and } B.$$

$$29. \text{ If } \tan\theta + \sin\theta = m, \text{ and } \tan\theta - \sin\theta = n \text{ show that } (m^2 - n^2) = 4\sqrt{mn}$$

$$30. \text{ Prove that } \frac{\sqrt{\sec\theta - 1}}{\sqrt{\sec\theta + 1}} + \frac{\sqrt{\sec\theta + 1}}{\sqrt{\sec\theta - 1}} = 2 \operatorname{cosec}\theta$$

$$31. \text{ prove that } \frac{1 + \cos\theta + \sin\theta}{1 + \cos\theta - \sin\theta} = \frac{1 + \sin\theta}{\cos\theta}$$

$$32. \text{ If } x = r \sin A \cos C, y = r \sin A \sin C \text{ and } z = r \cos A \text{ prove that } r^2 = x^2 + y^2 + z^2$$

Last date of submission 25th June 2016

Do it on the A-4 size ruled sheet

Attach one cover page showing Name ,class, subject and Title as Assignment.